**CENTRAL-EUROPEAN OLYMPIAD IN INFORMATICS** 



Sárospatak, Hungary 28 July - 4 August 2005

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English

Day 1: keys

## **Multi-key Sorting**

Input file: keys.in Output file: keys.out Source Code: keys.pas/.c/.cpp 100 points Time limit: 6 sec Memory limit:10 MB

Consider a table with rows and columns. The columns are numbered from 1 to C. For simplicity's sake, the items in the table are strings consisting of lower case letters.

Col. 1	Col. 2	Col. 3		Col. 1	Col. 2	Col. 3
apple	red	sweet		banana	brown	rotten
apple	green	sour		apple	green	sour
pear	green	sweet		pear	green	sweet
banana	yellow	sweet		apple	red	sweet
banana	brown	rotten		banana	yellow	sweet
Table 1			-	Table 2		

Col. 1	Col. 2	Col. 3			
apple	green	sour			
apple	red	sweet			
banana	brown	rotten			
banana	yellow	sweet			
pear	green	sweet			
Table 3					

You are given the operation Sort(k) on such tables: Sort(k) sorts the rows of a table in the order of the values in column k (while the order of the columns does not change). The sort is stable, that is, rows that have equal values in column k, remain in their original order. For example, applying Sort(2) to Table 1 yields Table 2.

We are interested in sequences of such sort operations. These operations are successively applied to the same table. For example, applying the sequence Sort(2); Sort(1) to Table 1 yields Table 3.

Two sequences of sort operations are called equivalent if, for any table, they have the same effect. For example, Sort(2); Sort(2); Sort(1) is equivalent to Sort(2); Sort(1). However, it is not equivalent to Sort(1); Sort(2), because the effect on Table 1 is different.

## Task

Given a sequence of sort operations, determine a shortest equivalent sequence.

## Input

The first line of the text file keys.in contains two integers, C and N. C  $(1 \le C \le 1\ 000\ 000)$  is the number of columns and N  $(1 \le N \le 3\ 000\ 000)$  is the number of sort operations. The second line contains N integers,  $k_i$   $(1 \le k_i \le C)$ . It defines the sequence of sort operations Sort( $k_1$ ); ...; Sort( $k_N$ ).

## Output

The first line of the text file keys.out contains one integer, M, the length of the shortest sequence of sort operations equivalent to the input sequence (Subtask A). The second line contains exactly M integers, representing a shortest sequence (Subtask B). You can omit the second line if you solve only Subtask A.

Example

keys.in	keys.out		
4 6	3		
1 2 1 2 3 3	1 2 3		